

$$\begin{aligned}\sin(\alpha+\beta) &= \sin\alpha\cos\beta + \cos\alpha\sin\beta \\ \sin(\alpha-\beta) &= \sin\alpha\cos\beta - \cos\alpha\sin\beta \\ \cos(\alpha+\beta) &= \cos\alpha\cos\beta - \sin\alpha\sin\beta \\ \cos(\alpha-\beta) &= \cos\alpha\cos\beta + \sin\alpha\sin\beta \\ \operatorname{tg}(\alpha+\beta) &= (\operatorname{tg}\alpha + \operatorname{tg}\beta) / (1 - \operatorname{tg}\alpha\operatorname{tg}\beta) \\ \operatorname{tg}(\alpha-\beta) &= (\operatorname{tg}\alpha - \operatorname{tg}\beta) / (1 + \operatorname{tg}\alpha\operatorname{tg}\beta)\end{aligned}$$

$$\begin{aligned}\sin(2a) &= 2\sin(a)\cos(a); \\ \cos(2a) &= \cos^2(a) - \sin^2(a) = 1 - 2\sin^2(a); \\ \operatorname{tg}(2a) &= 2\operatorname{tg}(a) / (1 - \operatorname{tg}^2(a)); \\ \operatorname{ctg}(2a) &= \operatorname{ctg}^2(a) - 1 / 2\operatorname{ctg}(a); \\ \sin(3a) &= 3\sin(a) - 4\sin^3(a); \\ \operatorname{tg}(3a) &= 3\operatorname{tg}(a) - \operatorname{tg}^3(a) / (1 - 3\operatorname{tg}^2(a)); \\ \operatorname{ctg}(3a) &= 3\operatorname{ctg}(a) - \operatorname{ctg}^3(a) / (1 - 3\operatorname{ctg}^2(a));\end{aligned}$$

$$\begin{aligned}\sin^2(a/2) &= (1 - \cos(a)) / 2; \\ \cos^2(a/2) &= (1 + \cos(a)) / 2; \\ \operatorname{tg}^2(a/2) &= (1 - \cos(a)) / (1 + \cos(a)); \\ \operatorname{ctg}^2(a/2) &= (1 + \cos(a)) / (1 - \cos(a)); \\ \operatorname{tg}(a/2) &= \sin(a) / (1 + \cos(a)) = (1 - \cos(a)) / \sin(a); \\ \operatorname{ctg}(a/2) &= \sin(a) / (1 - \cos(a)) = (1 + \cos(a)) / \sin(a);\end{aligned}$$

$$\begin{aligned}\sin(a) + \sin(b) &= 2\sin((a+b)/2)\cos((a-b)/2); \\ \sin(a) - \sin(b) &= 2\sin((a-b)/2)\cos((a+b)/2); \\ \cos(a) + \cos(b) &= 2\cos((a+b)/2)\cos((a-b)/2); \\ \cos(a) - \cos(b) &= -2\cos((a+b)/2)\sin((a-b)/2) = 2\cos((a+b)/2)\sin((b-a)/2); \\ \cos(a) + \sin(b) &= \sqrt{2}\cos(45^\circ - a); \\ \cos(a) - \sin(b) &= \sqrt{2}\sin(45^\circ - a); \\ \operatorname{tg}(a) + \operatorname{tg}(b) &= \sin(a+b) / (\cos(a)\cos(b)); \\ \operatorname{tg}(a) - \operatorname{tg}(b) &= \sin(a-b) / (\cos(a)\cos(b)); \\ \operatorname{ctg}(a) + \operatorname{ctg}(b) &= \sin(a+b) / (\sin(a)\sin(b)); \\ \operatorname{ctg}(a) - \operatorname{ctg}(b) &= \sin(b-a) / (\sin(a)\sin(b)); \\ \operatorname{tg}(a) + \operatorname{ctg}(b) &= \cos(a-b) / (\cos(a)\sin(b)); \\ \operatorname{tg}(a) - \operatorname{ctg}(b) &= -\cos(a+b) / (\cos(a)\sin(b)); \\ \operatorname{tg}(a) + \operatorname{ctg}(a) &= 2 / \sin(2a); \\ \operatorname{tg}(a) - \operatorname{ctg}(a) &= -2\operatorname{ctg}(2a);\end{aligned}$$

$$\begin{aligned}\sin(a)\sin(b) &= 1/2(\cos(a-b) - \cos(a+b)); \\ \cos(a)\cos(b) &= 1/2(\cos(a+b) + \cos(a-b)); \\ \sin(a)\cos(b) &= 1/2(\sin(a+b) + \sin(a-b));\end{aligned}$$

$$\begin{aligned}\sin(a) &= 2\operatorname{tg}(a/2) / (1 + \operatorname{tg}^2(a/2)); \\ \cos(a) &= (1 - \operatorname{tg}^2(a/2)) / (1 + \operatorname{tg}^2(a/2)); \\ \operatorname{tg}(a) &= 2\operatorname{tg}(a/2) / (1 - \operatorname{tg}^2(a/2)); \\ \operatorname{ctg}(a) &= (1 - \operatorname{tg}^2(a/2)) / 2\operatorname{tg}(a/2);\end{aligned}$$